

# Time for Networks: Mutation Testing for Timed Automata Networks

Gilles Perrouin

[gilles.perrouin@unamur.be](mailto:gilles.perrouin@unamur.be)

 @GPerrouin

FORMALISE 2024, Lisbon, Portugal, April 14th



# Time for Networks: Mutation Testing for Timed Automata Networks

David  
Cortés  
Jesus  
Aranda



James  
Ortiz



Davide  
Basile



Pierre-Yves  
Schobbens



# Timed Safety-critical Systems



TAP Air Portugal Website, 2024



Source:  
[https://en.wikipedia.org/wiki/Mechanical\\_ventilation#/media/File:Servo\\_I\\_Ventilator.jpg](https://en.wikipedia.org/wiki/Mechanical_ventilation#/media/File:Servo_I_Ventilator.jpg)

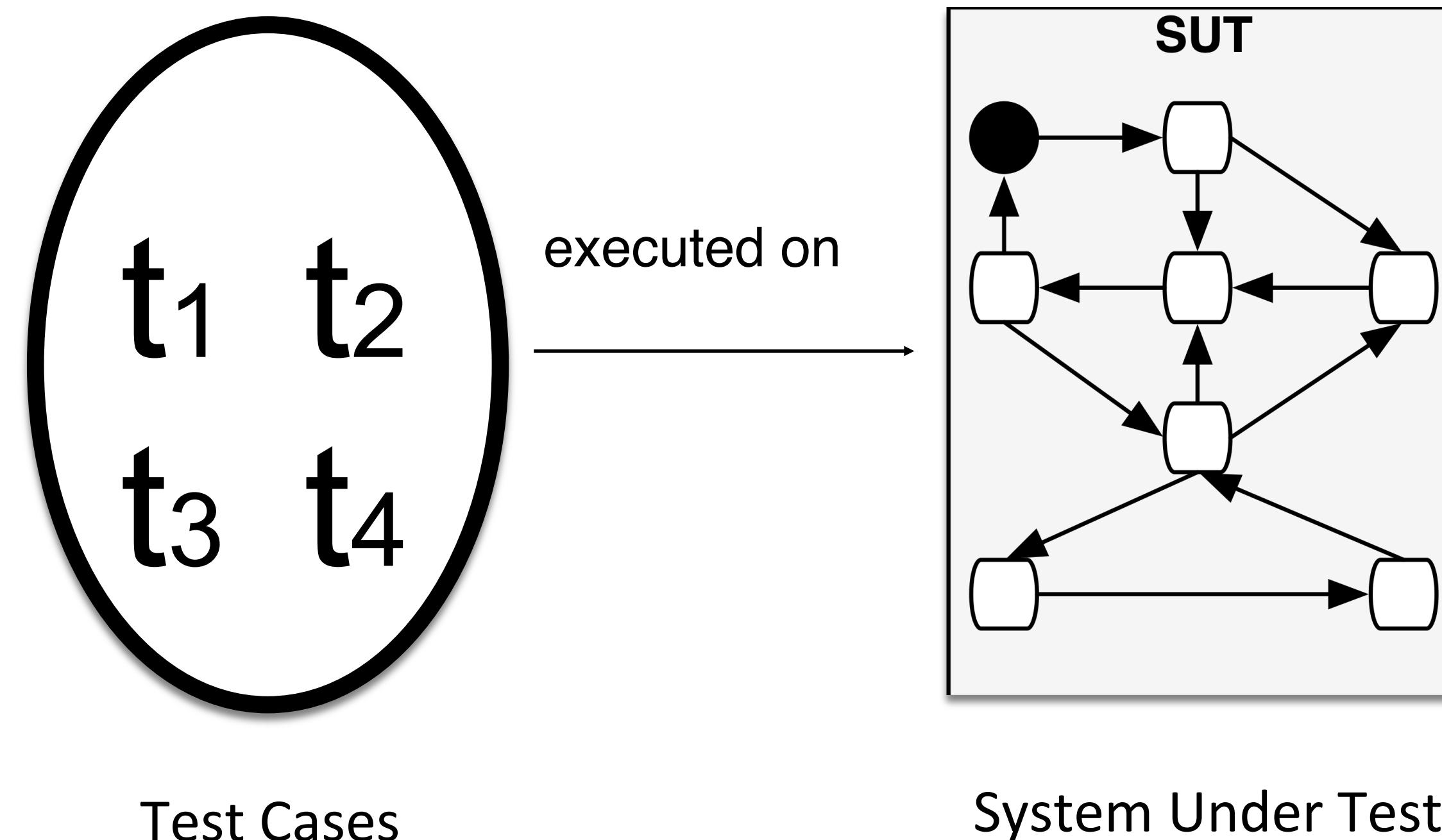


By Jcornelius - Own work, CC BY 2.5,  
<https://commons.wikimedia.org/w/index.php?curid=1475282>

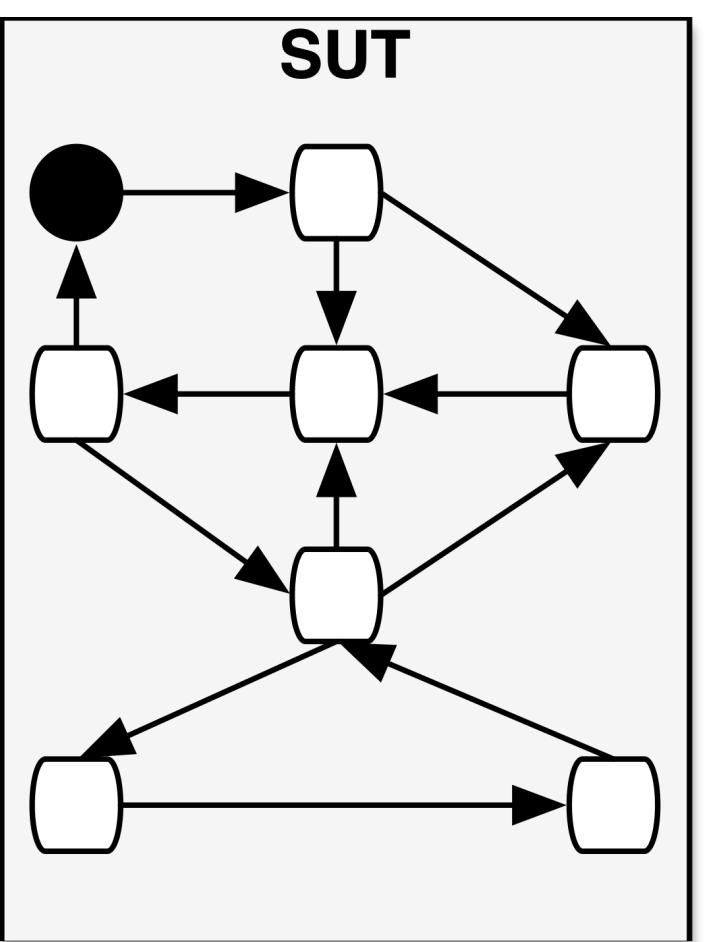
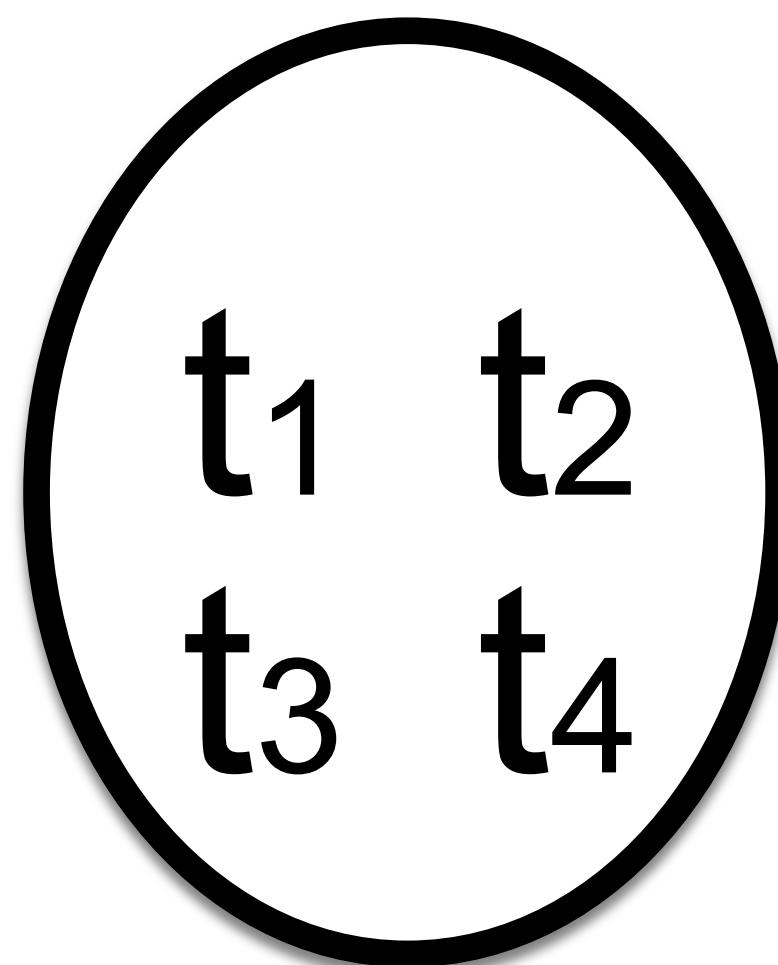
# Testing Timed Systems

Standards like DO-178 and ISO26262 require thorough testing of TS

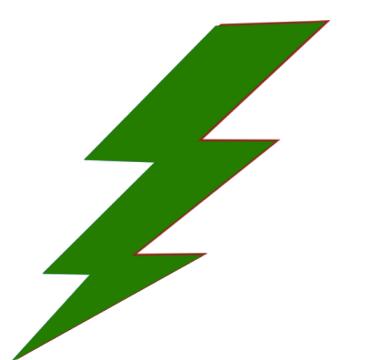
To ensure test quality, ***mutation testing*** can be used



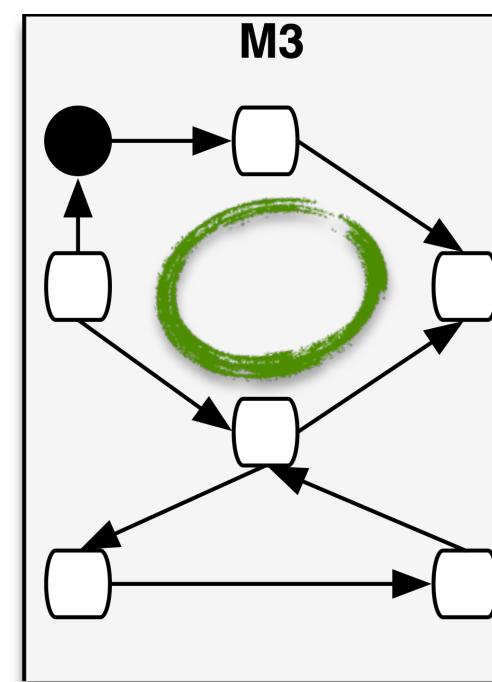
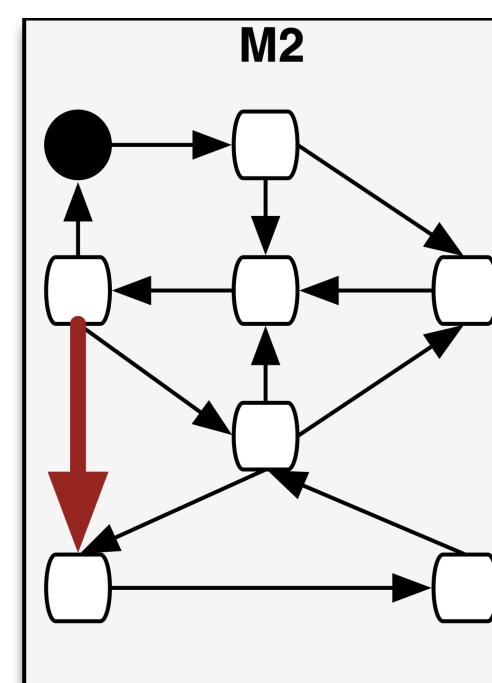
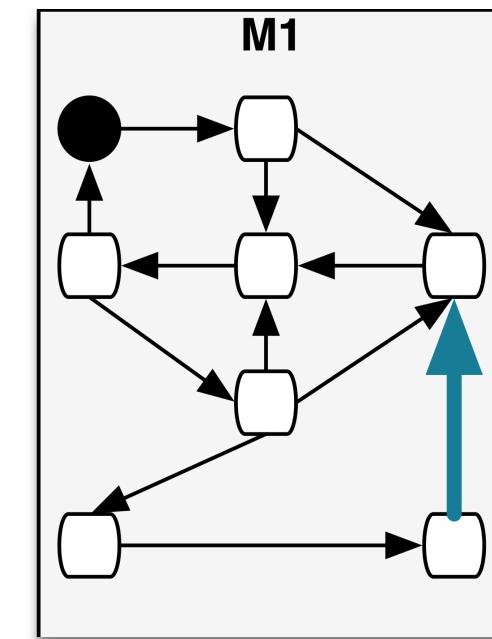
# Mutation Testing



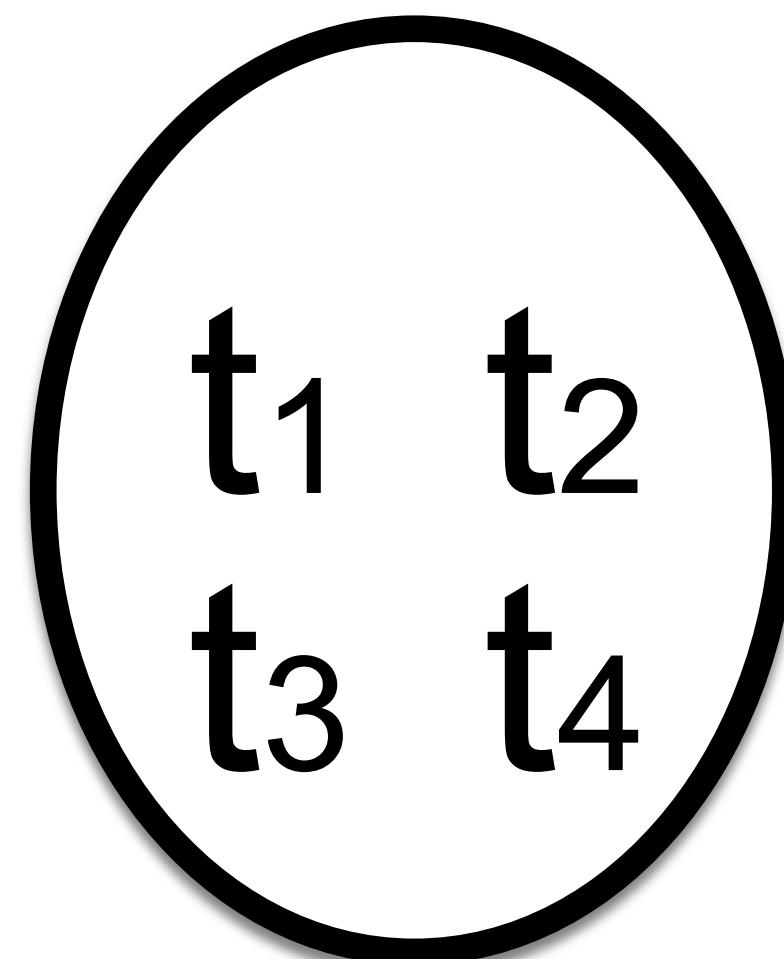
Mutation operator



Mutants



# Mutation Testing

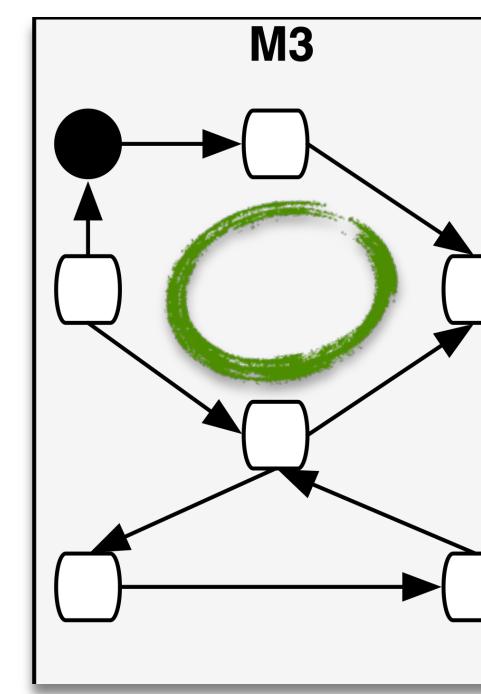
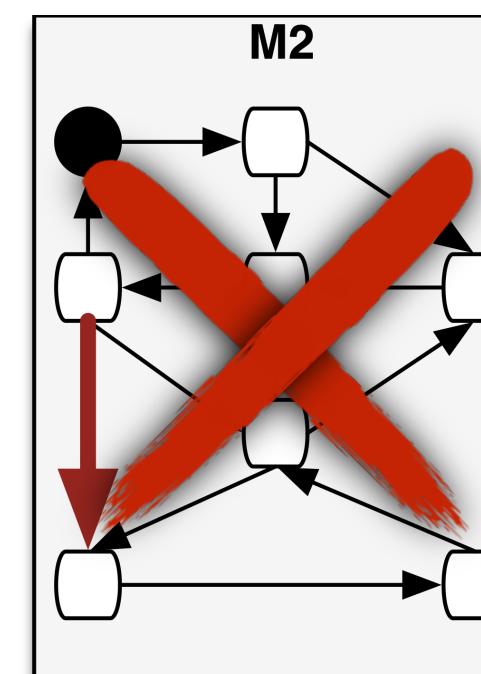
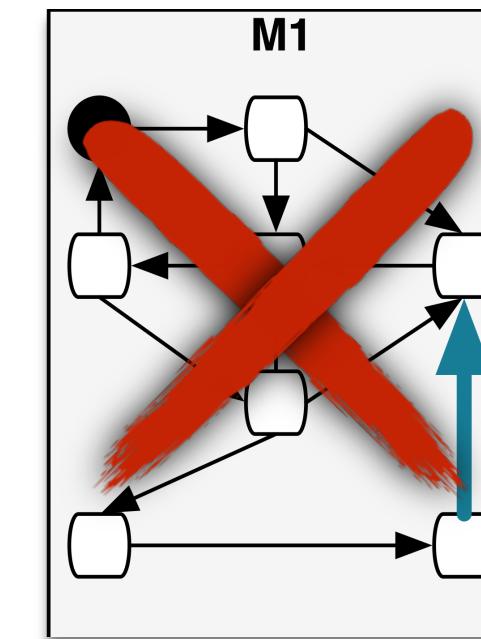


$$Score = \frac{\text{Killed mutants}}{\text{Total mutants}}$$

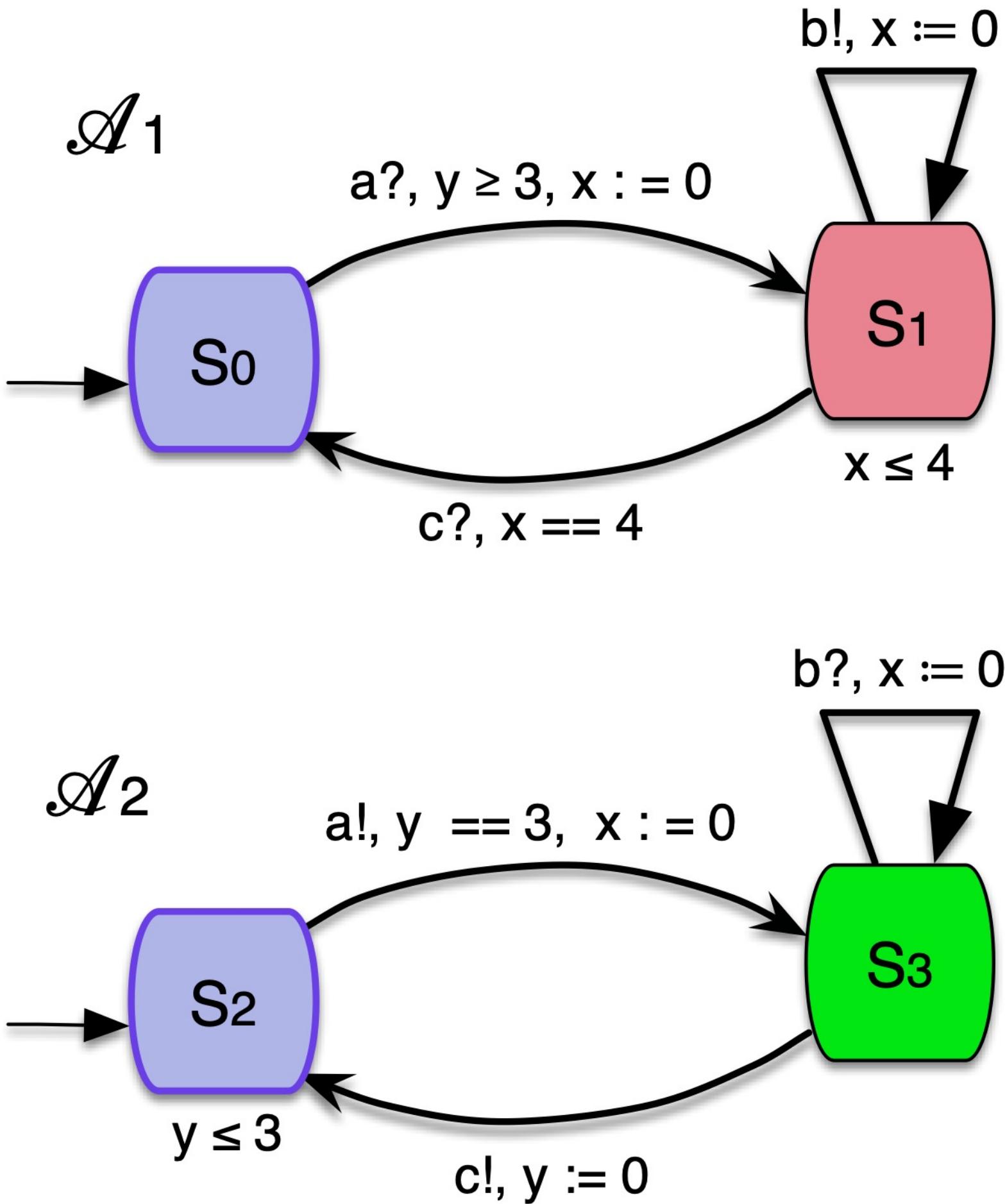
executed  
on

Mutation score = 2/3

Mutants



# Modelling (Distributed) Timed Systems



**Timed Automata with Input and Outputs: TAIO<sup>1</sup>**

**Network of Timed Automata (NTA):** Parallel product of TAIO where input is blocking and synchronization is broadcast (one sender, zero or more receivers)

1. Kaynar, D., Lynch, N., Segala, R., & Vaandrager, F. (2010). *The theory of timed I/O automata*. Morgan & Claypool Publishers.

# Mutation Operators for Timed Automata

| Nilsson <i>et al.</i> [38] |                        | Aichernig <i>et al.</i> [2] |                  | Basile <i>et al.</i> [7] |                     |
|----------------------------|------------------------|-----------------------------|------------------|--------------------------|---------------------|
| Op                         | Description            | Op                          | Description      | Op                       | Description         |
| ET                         | Execution time         | CA                          | Change action    | TMI                      | Transition missing  |
| IAT                        | Inter-arrival time     | CT                          | Change target    | TAD                      | Transition ADD      |
| PO                         | Pattern offset         | CS                          | Change source    | SMI                      | State missing       |
| LT                         | Lock time              | CG                          | Change guard     | CXL                      | Constant exchange L |
| UT                         | Unlock time            | NG                          | Negate guard     | CXS                      | Constant exchange S |
| HTS                        | Hold time shift        | CI                          | Change invariant | CCN                      | Constraint negation |
| PC                         | Precedence constraints | SL                          | Sink location    | -                        | -                   |
| -                          | -                      | IR                          | Invert reset     | -                        | -                   |

## Mutation-based Testing Criteria for Timeliness

Robert Nilsson<sup>†</sup>  
<sup>†</sup>Department of Computer Science  
 University of Skövde, Box 408SE  
 541 28 Skövde, Sweden  
 {robert,stef}@ida.his.se

Jeff Offutt<sup>\*</sup>  
<sup>\*</sup>Department of Information and Software Engineering  
 George Mason University  
 Fairfax, VA 22030 USA  
 ofut@ise.gmu.edu

## Time for Mutants — Model-Based Mutation Testing with Timed Automata

Bernhard K. Aichernig , Florian Lorber , and Dejan Nićković

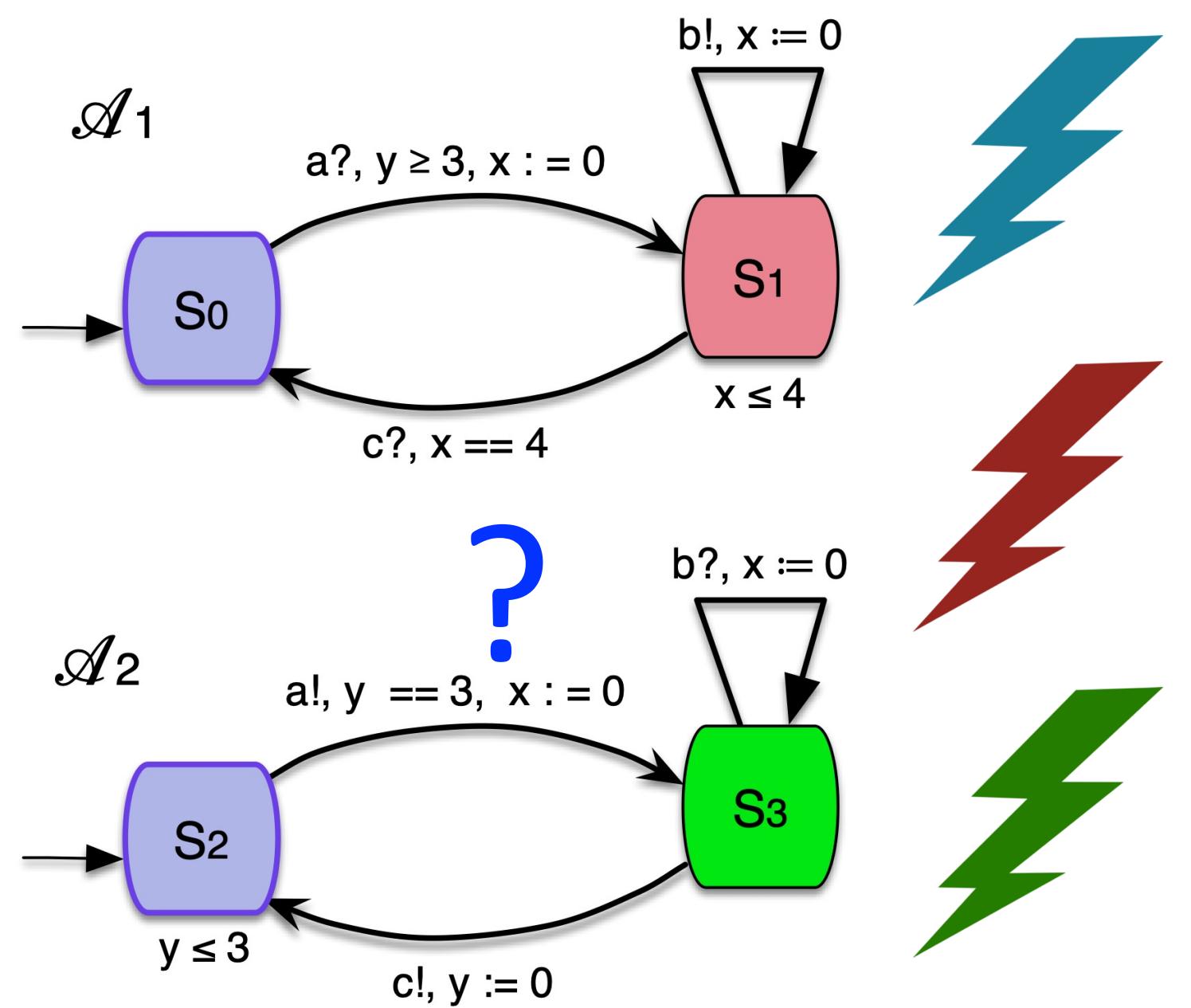
## Tackling the Equivalent Mutant Problem in Real-Time Systems: The 12 Commandments of Model-Based Mutation Testing

Davide Basile, Maurice H. ter Beek, Maxime Cordy, Axel Legay

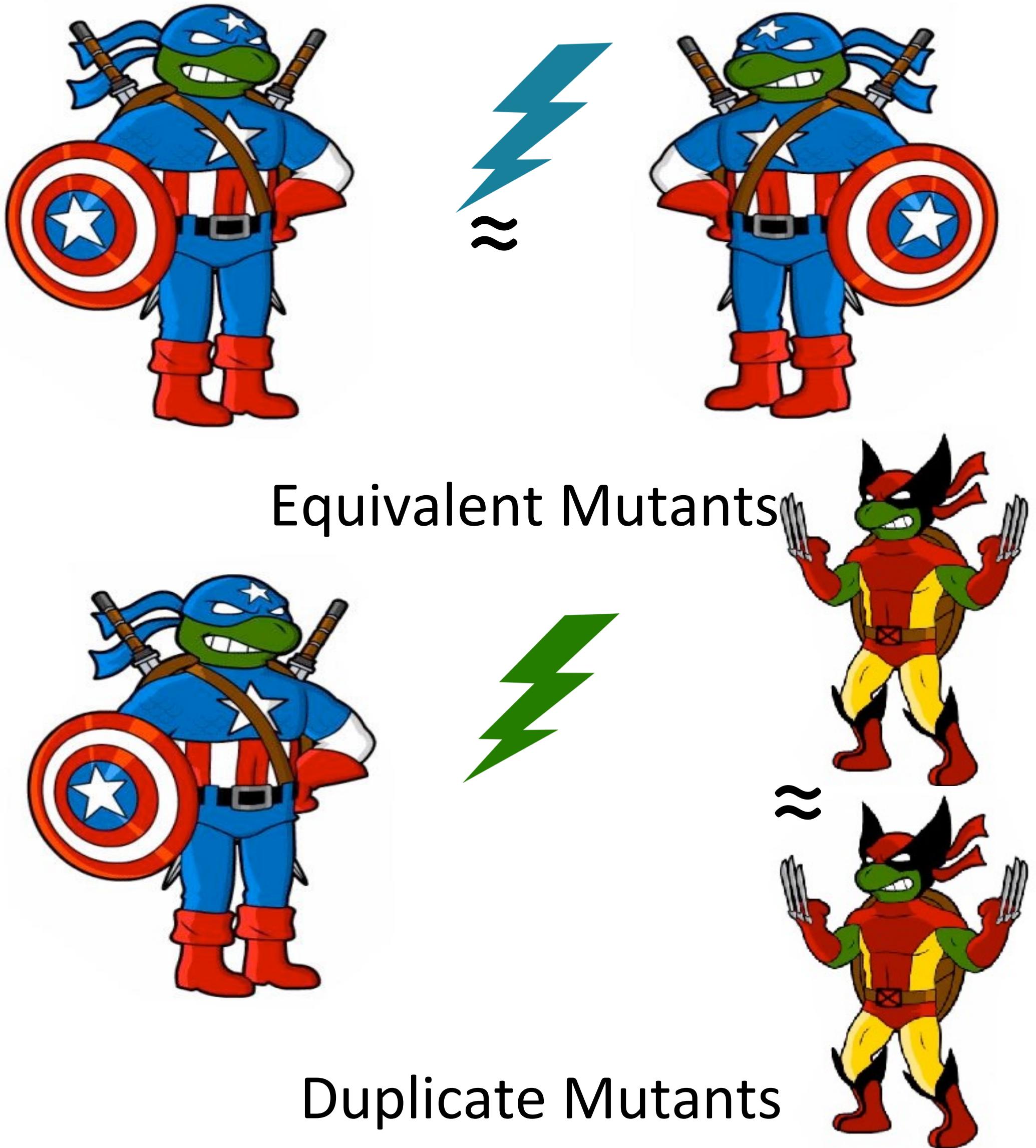
Timed Automata with  
 Task model

Timed Automata with  
 Input and Output

# Motivation



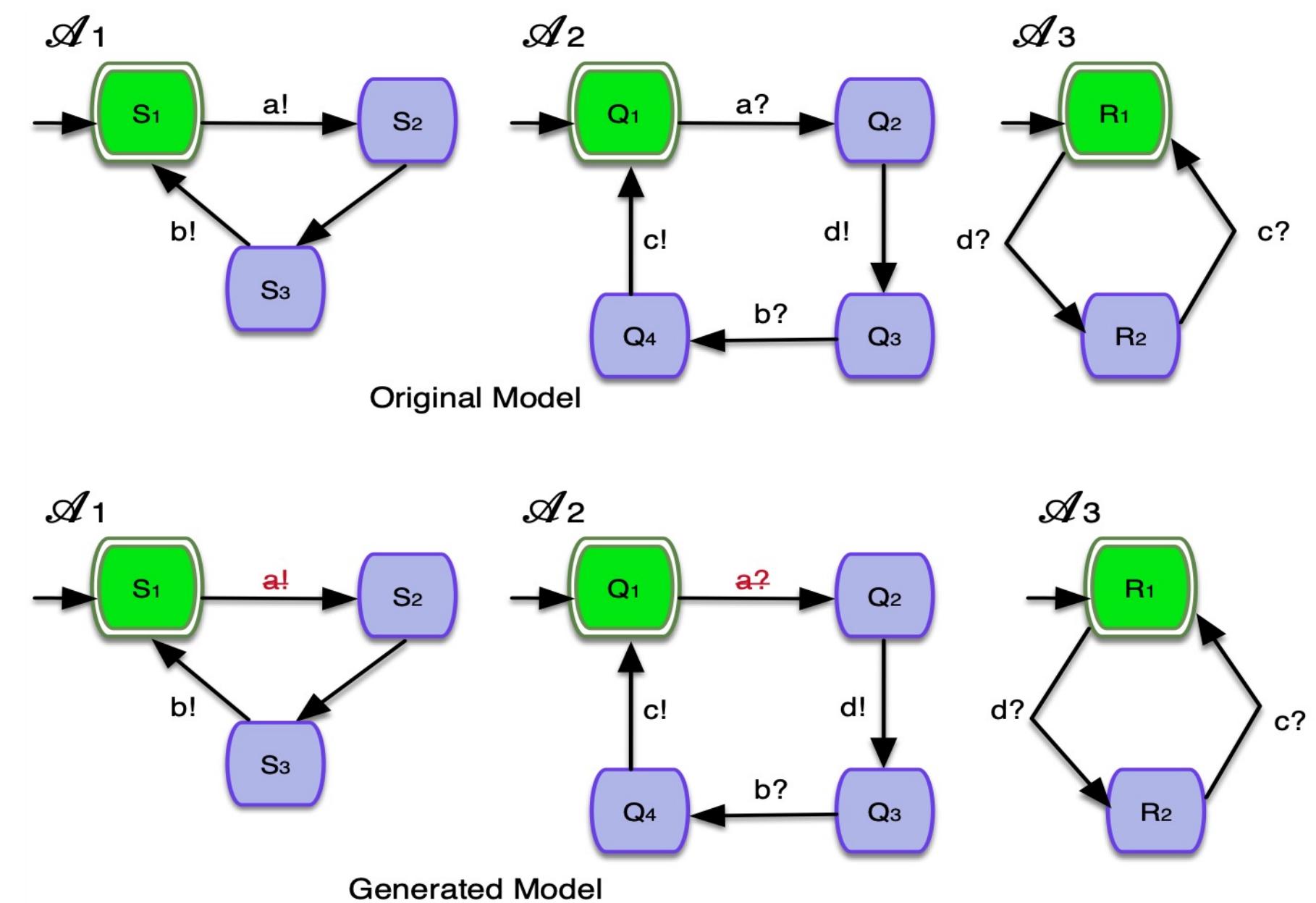
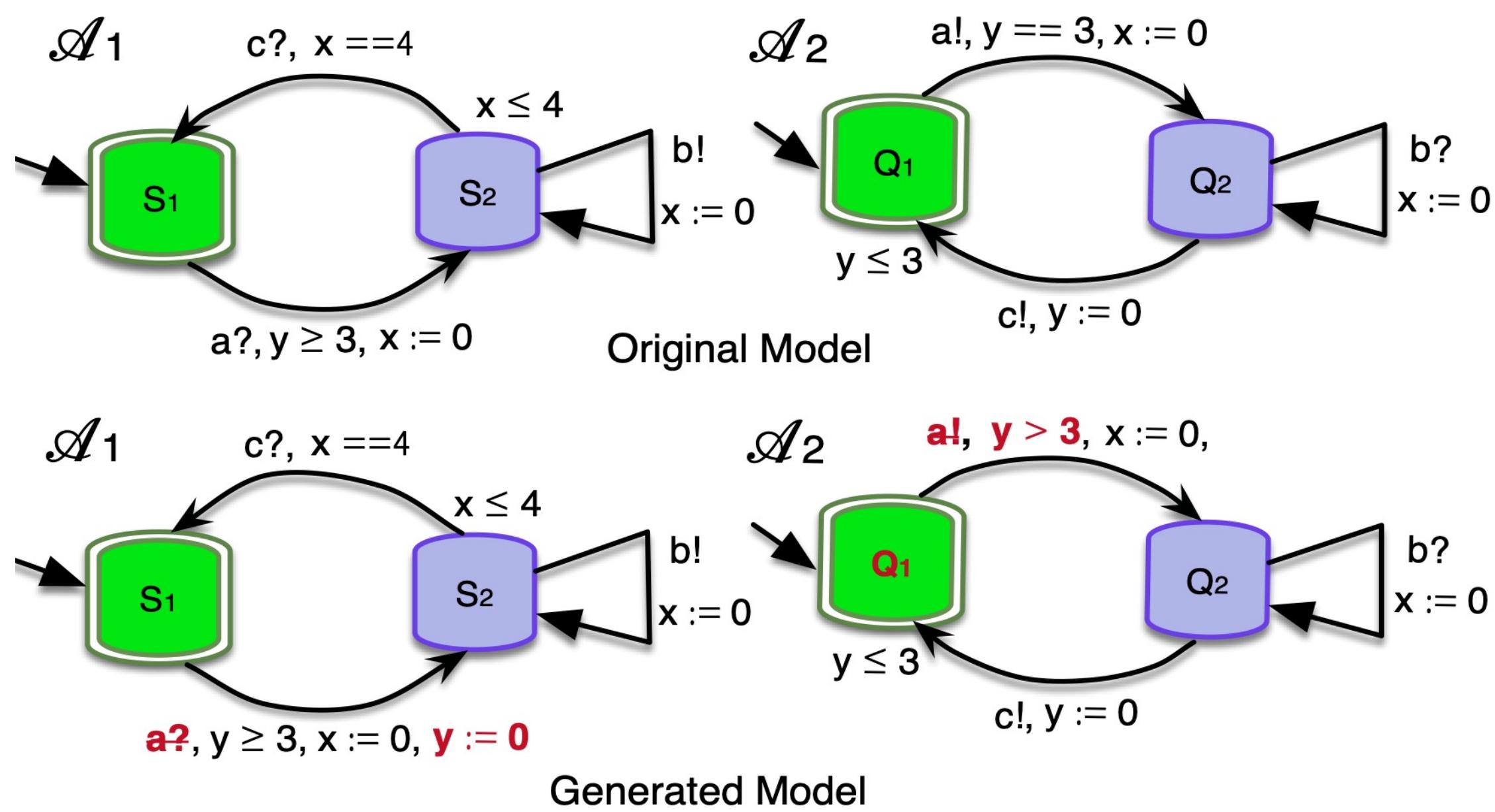
Existing operators do not focus on  
NTA



# Mutation Operators for NTA

|       | Name             | Acronym | Type                  |
|-------|------------------|---------|-----------------------|
| NTAIO | <i>syncSeq</i>   | SS      | Sequential            |
|       | <i>delSync</i>   | DS      | Interleave            |
|       | <i>maskVarh</i>  | MVCh    | Shadow global channel |
|       | <i>maskVarc</i>  | MVCc    | Shadow global clock   |
|       | <i>urgChan</i>   | UC      | Urgent Channel        |
|       | <i>BroadChan</i> | BC      | Broadcast Channel     |
| TAIO  | <i>urgLoc</i>    | UL      | Urgent Location       |
|       | <i>commLoc</i>   | CL      | Committed Location    |

# Synchronisation Operators



**SyncSeq.** Forces sequential behaviour by removing synchronisation events and commits a source location.

**DelSeq.** Removes synchronisation

# Masking Operators

```
clock time; Global declarations
```

```
int[0,100] foo=0; local declarations
```

Original Model

```
clock time; Global declarations
```

```
int[0,100] foo=0; local declarations  
clock time; <- Mutation
```

Generated Model

**MV $Cc$  (or MV $Cl$ ).** Masks a global clock by introducing a local clock with the same name.

**MV $Ch$ .** Similar mutation but for channels (not shown here)

# Channel Operators

```
chan go;  
clock x;
```

Global declarations

```
broadcast chan go;  
clock x;          Global declarations
```

Original Models

```
broadcast chan go;  
clock x;          Global declarations
```

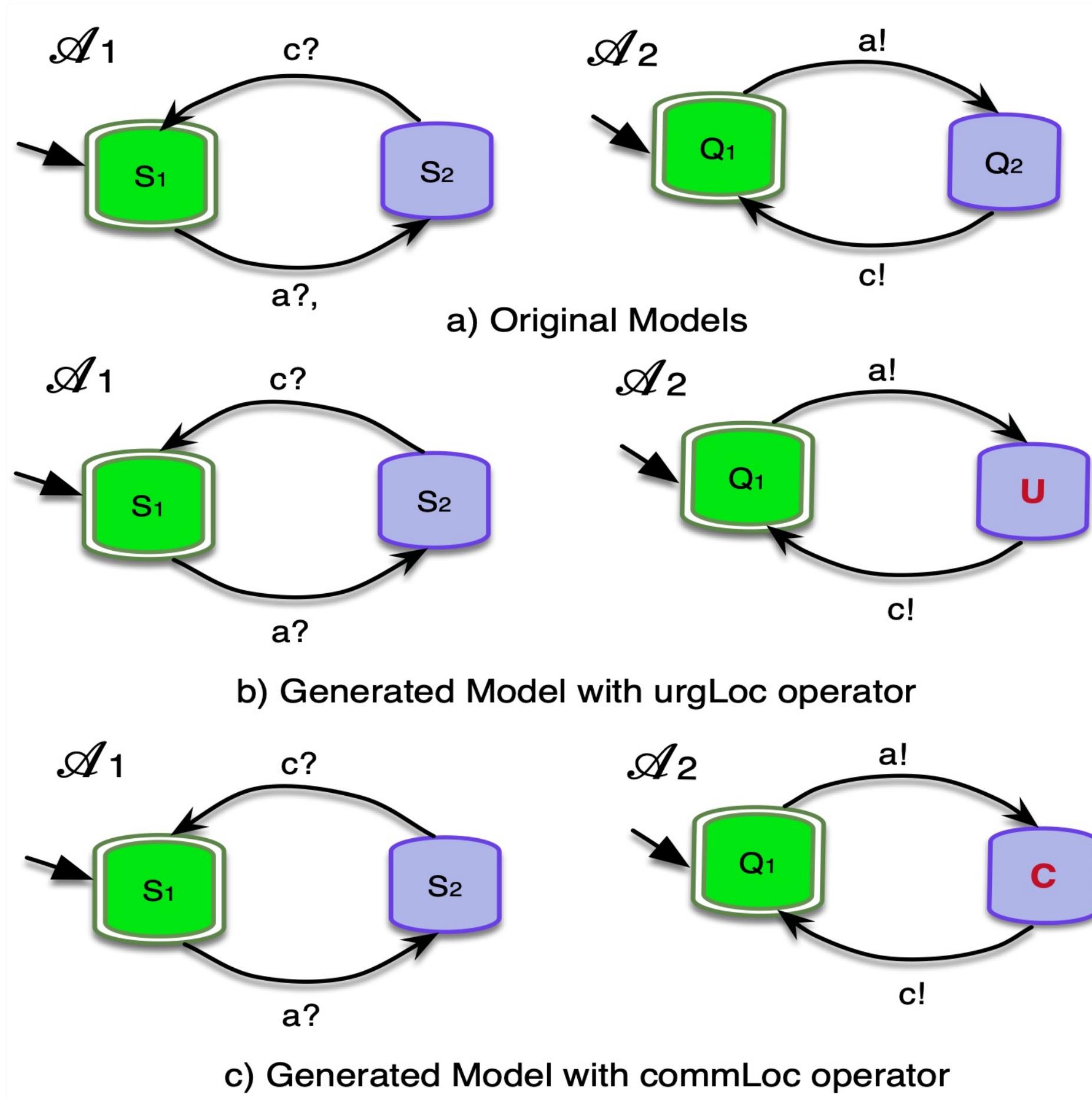
```
broadcast urgent chan go;  
clock x;          Global declarations
```

Generated Models

**BroadChan.** Transforms an unicast channel into a broadcast one

**UrgChan.** Make the channel urgent (prevent delays and encourage synchronisation)

# Location Operators



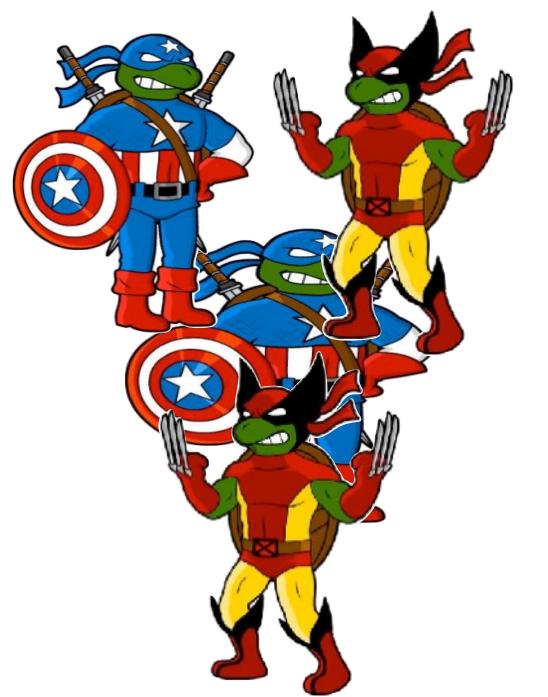
**UrgLoc.** Make location as Urgent (no time can be waited for)

**CommLoc.** Make location as committed (freezes time)

# Tackling Timed Mutants' Uselessness



Davide Basile *et al.* ***Tackling the equivalent mutant problem in real-time systems: the 12 commandments of model-based mutation testing.*** In SPLC'20: 24th ACM International Systems and Software Product Line Conference

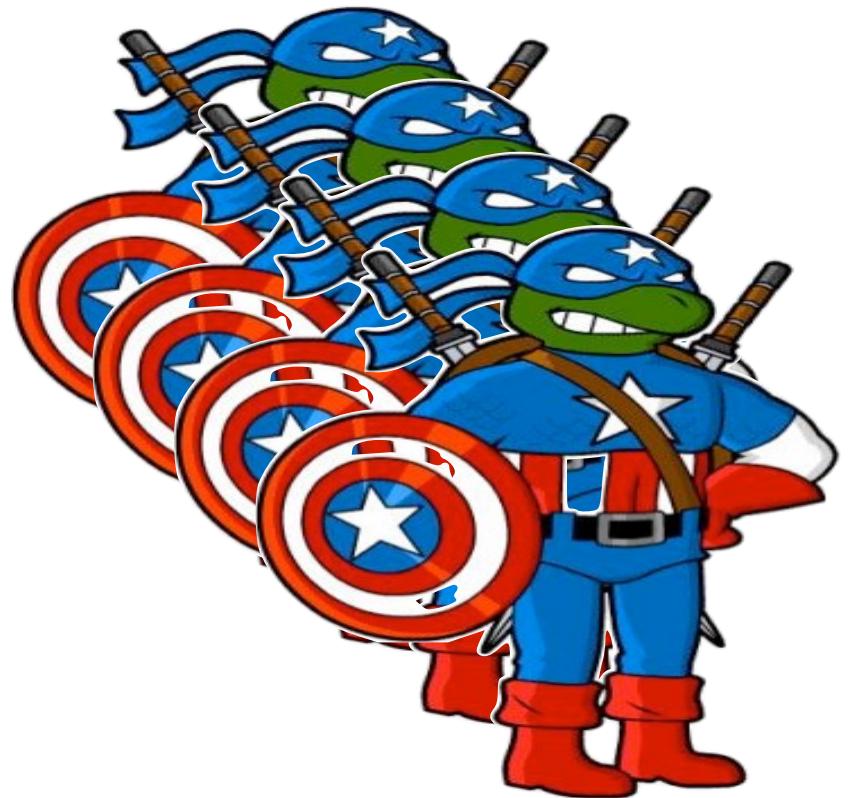


Davide Basile *et al.* ***Static detection of equivalent mutants in real-time model-based mutation testing: An Empirical Evaluation.*** Empirical Software Engineering 27, 7 (2022), 160.



Jaime Cuartas *et al.* ***MUPPAAL: Reducing and Removing Equivalent and Duplicate Mutants in UPPAAL.*** In 2023 IEEE International Conference on Software Testing, Verification and Validation Workshops (ICSTW). IEEE, 52–61

# Research Questions



RQ1. How many mutants?



RQ2. TAIIO vs NTAIO Operators  
(Equivalent Mutants)



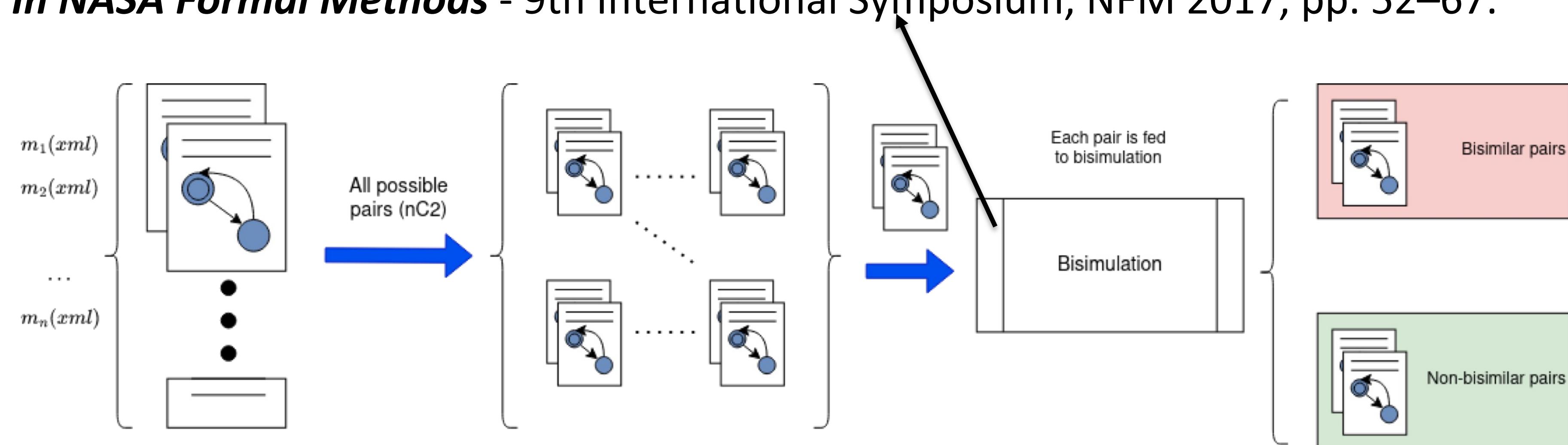
RQ3. TAIIO vs NTAIO Operators  
(Duplicate Mutants)



RQ4. Bisimulation Costs

# Evaluation

James Jerson Ortiz, et al. 2017. *Multi-timed Bisimulation for Distributed Timed Automata*. In *NASA Formal Methods* - 9th International Symposium, NFM 2017, pp. 52–67.



Jaime Cuartas et al. *MUPPAAL: Reducing and Removing Equivalent and Duplicate Mutants in UPPAAL*. In 2023 IEEE International Conference on Software Testing, Verification and Validation Workshops (ICSTW). IEEE, 52–61



# Case Studies



Collision Avoidance (CA)

Locations: 12

Transitions: 26



Train Gate Controller (TGC)

Locations: 17

Transitions: 16



Tram Door (TD)

Locations: 32

Transitions: 36



Gear Controller (GC)

Locations: 48

Transitions: 30



Mechanical Ventilator (MV)

Locations: 24

Transitions: 29

# RQ1. How Many Mutants?

|              | CA | GC  | TGC | MV  | TD  |
|--------------|----|-----|-----|-----|-----|
| <b>DS</b>    | 25 | 56  | 36  | 17  | 36  |
| <b>MVCh</b>  | 22 | 40  | 16  | 60  | 55  |
| <b>MVCl</b>  | 2  | 2   | 7   | 9   | 8   |
| <b>UC</b>    | 11 | 20  | 8   | 12  | 11  |
| <b>UL</b>    | 12 | 46  | 28  | 17  | 36  |
| <b>CL</b>    | 12 | 46  | 28  | 20  | 31  |
| <b>SS</b>    | 9  | 18  | 7   | 7   | 10  |
| <b>BC</b>    | 0  | 0   | 0   | 7   | 0   |
| <b>Total</b> | 93 | 228 | 130 | 149 | 179 |

The Delete Synchronisation operator ***is the most applicable to our cases*** ( $170/779 \approx 21\%$ )

The Broadcast Channel is ***only applicable to MV*** since all the other cases already have a broadcast channel ( $7/779 \approx 0.8\%$ )

A ***diverse set*** of mutant operators applicable to various (N)TAIO constructs

# RQ2. Mutant Equivalence

| Case  | Collision Avoidance | Gear Control  | Train Gate Controller | Mechanical Ventilator | Tram Door    | Average |
|-------|---------------------|---------------|-----------------------|-----------------------|--------------|---------|
| DS    | 4/25 (16%)          | 9/56 (16%)    | 3/36 (8%)             | 15/17 (88%)           | 1/36 (3%)    | 26%     |
| MVCh  | 3/22 (14%)          | 38/40 (95%)   | 14/16 (87%)           | 56/60 (93%)           | 36/55 (65%)  | 71%     |
| MVCc  | 0/2 (0%)            | 1/2 (50%)     | 4/7 (57%)             | 6/9 (66%)             | 3/8 (37%)    | 42%     |
| UC    | 5/11 (45 %)         | 19/20 (95%)   | 5/8 (62%)             | 8/12 (66%)            | 6/11 (54%)   | 64%     |
| UL    | 4/12 (33%)          | 43/46 (93%)   | 21/28 (75%)           | 6/17 (35%)            | 24/36 (66%)  | 60%     |
| CL    | 3/12 (25%)          | 43/46 (93%)   | 21/28 (75%)           | 9/20 (45%)            | 20/31 (64%)  | 60%     |
| SS    | 0/9 (0%)            | 1/18 (5%)     | 0/7 (0%)              | 4/7 (57%)             | 0/10 (0%)    | 12%     |
| BC    | 0 (0%)              | 0 (0%)        | 0 (0%)                | 2/7 (28%)             | 0 (0%)       | 28%     |
| Total | 19/93 (20%)         | 154/228 (67%) | 75/130 (58%)          | 106/149 (71%)         | 90/187 (48%) | 52%     |

The masking channel operator is the ***highest contributor*** to equivalent mutants

This ***is not true*** for the other masking operator (MVCc)

NTAIO mutation operators ***either generate the lowest or the highest numbers*** of equivalent mutants

## RQ3. Mutant Duplicates

| Case                  | Most Duplicated Operator per pair type  |
|-----------------------|---|
| Collision Avoidance   | MVCh (5/7)                              |
| Gear Controller       | CL (2/7), UL (2/7), CL & UL (3/7)       |
| Train Gate Controller | CL (2/7), UL (2/7), CL & UL (3/7)       |
| Mechanical Ventilator | MVCh (6/7)                              |
| Tram Door             | MVCh (4/6) (MVCc did yield 0 duplicate) |

***MVCh is the largest contributor*** to duplicate pairs

***« Location » (UL and CL) operators contribute equally***

## RQ4. Computational Costs

| Case study | Mutant generation | Bisimulation of all pairs | Bisimulation per pair    |
|------------|-------------------|---------------------------|--------------------------|
| CA         | 1 s               | 24 min                    | $660 \pm 41$ ms          |
| GC         | 3 s               | 172 min                   | $1 \text{ s} \pm 126$ ms |
| TGC        | 2 s               | 153 min                   | $748 \pm 52$ ms          |
| MV         | 2.5 s             | 165 min                   | $1 \text{ s} \pm 177$ ms |
| TD         | 3 s               | 195 min                   | $726 \pm 67$ ms          |

Mutant generation is fast (as expected)

Overall comparisons can take *more than 3 hours* for Tram Door...

...but on average *timed bisimulation takes less than 1s per comparison*

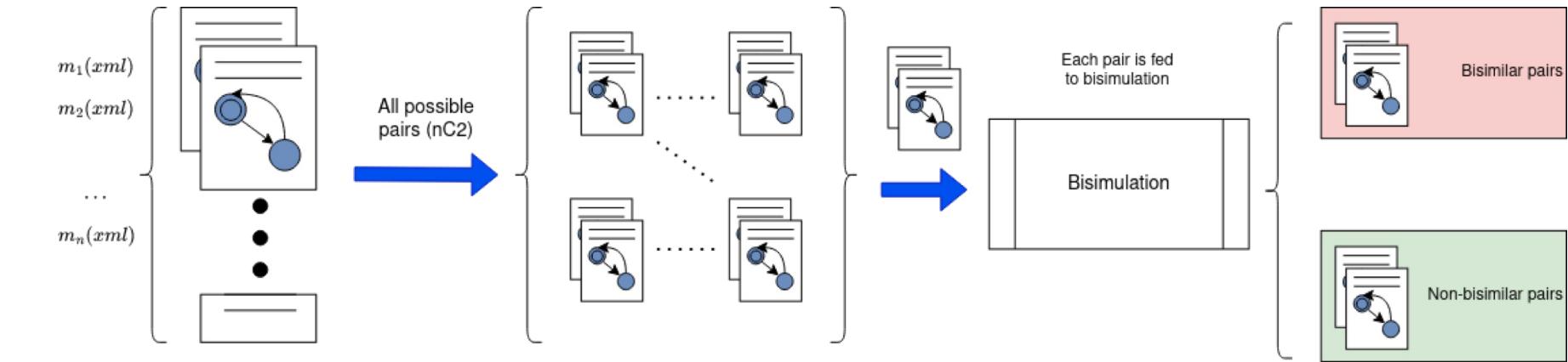
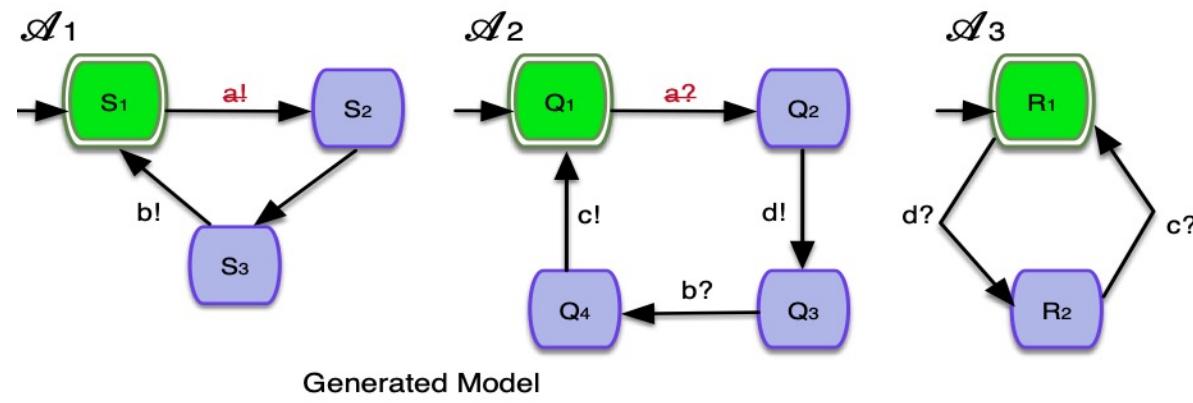
# Discussion

**Number of equivalent mutants.** Quite high, influenced by resets for MVCh operator.

**Static detection of mutants.** Static detection of equivalent mutants could save time for some mutant operators. The influence of resets is hard to detect statically. Precision/speed tradeoff to investigate.

**Timed Bisimulation for mutant equivalence.** Strongest relation that allows us to distinguish subtle behavioural faults. We would like to see the influence of other relations (TIOCO, ...) in the future.

**Stubbornness.** Studies are required to see how useful are mutants and how hard they are to kill in practice.



## 8 mutation operators for *NTAIO*

Mutation framework based on  
MUPPAAL



5 cases studies



**Diversity of behaviours** regarding  
equivalents/duplicates  
Timed bisimulation **scales**



GitLab



# Time for Networks: Mutation Testing for Timed Automata Networks

Backup Slides

FORMALISE 2024, Lisbon, Portugal, April 14th



# Case Studies Details

| Case Studies | Instances | Locations | Transitions | Clocks | Channels | Broad. Channels | Urg. Channels |
|--------------|-----------|-----------|-------------|--------|----------|-----------------|---------------|
| CA           | 2         | 12        | 26          | 1      | 0        | 11              | 0             |
| GC           | 2         | 48        | 60          | 1      | 0        | 20              | 0             |
| TGC          | 3         | 17        | 18          | 1      | 0        | 9               | 0             |
| MV           | 5         | 24        | 29          | 6      | 7        | 12              | 0             |
| TD           | 5         | 32        | 36          | 2      | 0        | 11              | 0             |



Jaime Cuartas, et al.. ***Formal Verification of a Mechanical Ventilator using UPPAAL***. In Proceedings of the 9th ACM SIGPLAN International Workshop on Formal Techniques for Safety-Critical Systems (FTSCS 2023). Association for Computing Machinery, New York, NY, USA, 2–13.  
<https://doi.org/10.1145/3623503.3623536>

# Mutant Duplicates (per case study)

**Table 6: Average redundant mutants for the CA case study.**

| Operator | No. duplicated pairs | Most duplicated operator |
|----------|----------------------|--------------------------|
| DS       | 56 / 8556 (0.65%)    | MVCH 10 (27%)            |
| MVCh     | 1055 / 8556 (12.3%)  | CL & UL 528 (50%)        |
| MVCI     | 116 / 8556 (1.3%)    | MVCH 44 (38%)            |
| UC       | 591 / 8556 (7%)      | MVCH 242 (40%)           |
| UL       | 639 / 8556 (7.5%)    | MVCH 264 (41%)           |
| CL       | 636 / 8556 (7.5%)    | MVCH 264 (42%)           |
| SS       | 0 / 8556(0%)         | N/A                      |

**Table 7: Average duplicate mutants for the TGC case study.**

| Operator | No. duplicated pairs | Most duplicated operator |
|----------|----------------------|--------------------------|
| DS       | 643 / 16770 (4%)     | UL 153 (23%)             |
| MVCh     | 1292 / 16770 (8%)    | CL & UL 896 (69%)        |
| MVCI     | 354 / 16770 (2%)     | CL & UL 224 (63%)        |
| UC       | 680 / 16770 (4%)     | CL & UL 448 (65%)        |
| UL       | 2107 / 16770 (12.5%) | CL 784 (37%)             |
| CL       | 2108 / 16770 (12.5%) | UL 784 (37%)             |
| SS       | 28 / 16770 (0.1%)    | CL 12 (42%)              |

**Table 8: average duplicate pairs of mutants for each operator, with the TD case study.**

| Operator | No. duplicated pairs  | Most duplicated operator |
|----------|-----------------------|--------------------------|
| DS       | 44 / 31,862 (0.1%)    | MVCH 14 (31%)            |
| MVCh     | 5569 / 31,862 (17.5%) | UL 1705 (30%)            |
| UC       | 1356 / 31,862 (4.2%)  | MVCH 605 (44%)           |
| UL       | 3509 / 31,862 (11%)   | MVCH 1705 (48%)          |
| CL       | 3511 / 31,862 (11%)   | MVCH 1704 (48%)          |
| SS       | 3 / 31,862 (0.009%)   | CL 1 (33%)               |

**Table 9: Average duplicate pairs of mutants for each operator, with the GC case study.**

| Operator | No. duplicated pairs  | Most duplicated operator |
|----------|-----------------------|--------------------------|
| DS       | 939 / 51,756 (1.8%)   | CL 167 (17%)             |
| MVCh     | 5515 / 51,756 (10.6%) | CL & UL 3680 (66%)       |
| MVCI     | 316 / 51,756 (0.6%)   | CL & UL 184 (58%)        |
| UC       | 2971 / 51,756 (5.7%)  | CL & UL 1840 (62%)       |
| UL       | 6221 / 51,756 (12%)   | CL 2116 (34%)            |
| CL       | 6221 / 51,756 (12%)   | UL 2116 (34%)            |
| SS       | 193 / 51,756 (0.3%)   | UL 58 (30%)              |

# Mutant Duplicates (MV)

**Table 10: Average duplicate pairs of mutants for each operator, with the MV case study.**

| Operator | No. duplicated pairs  | Most duplicated operator |
|----------|-----------------------|--------------------------|
| DS       | 2448 / 22,052 (11%)   | CL 167 (17%)             |
| MVCh     | 4837 / 22,052 2 (22%) | MVCH 1546 (31%)          |
| MVCI     | 972 / 22,052 (4.4%)   | MVCH 504 (51%)           |
| UC       | 1278 /22,052 (5.7%)   | MVCH 672 (52%)           |
| UL       | 909 / 22,052 (4.1%)   | MVCH 379 (41%)           |
| CL       | 1225 / 22,052 (5.5%)  | MVCH 548 (44%)           |
| BC       | 128 / 22,052 (0.5%)   | MVCH 55 (42%)            |
| SS       | 685 / 22,052 (3.1%)   | MVCH 340 (49%)           |